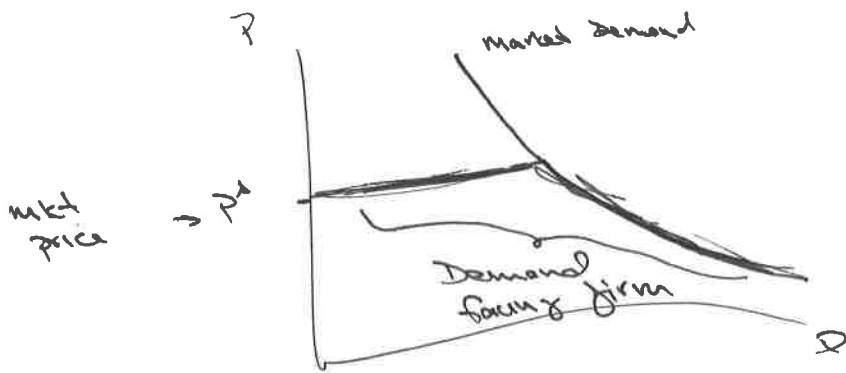


# Chapter 23 - Firm Supply

## The Economic Environment

- Demand taken as given
  - demand represents a constraint on the firm
  - the firm can't sell more than people demand
  - we need to distinguish between the market demand curve (what all firms together can sell) from the ~~firm's~~ demand curve facing the firm

- We'll assume markets are competitive
  - e.g. there are a large number of consumers and producers and so each take prices as given
  - why are firms price takers?
    - think about the demand curve each firm faces. If that firm changes more than others for the good, how many does it sell?
    - And if it changes less than all other firms? It captures the entire market



# The competitive firm's problem

→ Since the competitive firm takes prices as given, its problem is simply to choose the quantity to produce that maximizes profits.

That is:

$$\begin{aligned} \max_y & \quad Py - c(y) \\ \text{s.t.} & \quad y \geq 0 \end{aligned}$$

The FOC:

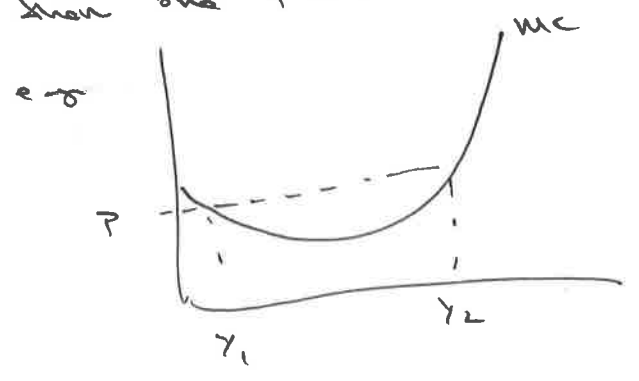
$$\frac{\partial \pi}{\partial y} = P - \underbrace{\frac{\partial c(y)}{\partial y}}_{= MC(y)} = 0$$

$$\Rightarrow P = MC(y)$$

the optimal choice of  $y$  satisfies this

→ 2 exceptions:

1) The MC curve could equal  $P$  at more than one point



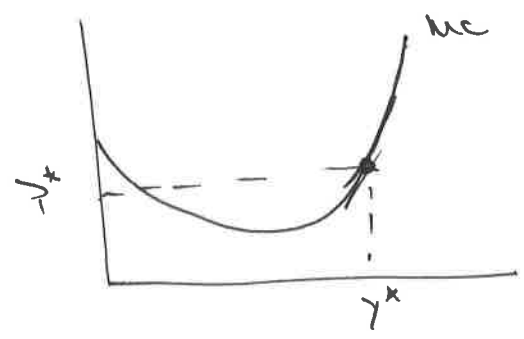
In this case, one needs to use the 2nd order condition:

$$\frac{\partial^2 \Pi}{\partial y^2} \leq 0$$

$$\Rightarrow -\frac{\partial MC(y)}{\partial y} \leq 0$$

$$\Rightarrow \frac{\partial MC(y)}{\partial y} \geq 0$$

the maximum will be where price = MC and where MC is increasing



2) The MC might not equal price for any positive level of output

→ in this case, the constraint,  $y \geq 0$ , binds

→ so the firm "shuts down"

→ when a firm shuts down, it still has to pay fixed costs,  $F$ , but not variable costs.

→ Thus the shutdown condition is

$$-F \geq p y - c_y(y) - F$$

if this, then shutdown (i.e. set  $y=0$ )

This condition can be rewritten as

$$0 > py - c_v(y)$$

$$\Rightarrow c_v(y) > py$$

$$\Rightarrow \frac{c_v(y)}{y} > p$$

$$\Rightarrow \underbrace{AVC(y)} > p$$

if  $AVC(y) > \text{price}$ , then better

off producing zero

→ price doesn't even cover  
variable costs

"We lose money on every sale,  
but make it up with volume."

→ so check shutdown and 2nd  
order conditions after final  
y where  $p = MC(y)$

→ The solution to the problem will  
be the supply function:  $y(p)$ .

→ but we might also want the  
inverse supply function, which  
gives price as a function of  
quantity. This is directly given  
from the FC:  $p = MC(y)$

Example: let  $c(y) = y^2$

$$\pi = py - y^2$$

$$\frac{d\pi}{dy} = p - 2y = 0$$

$$\begin{aligned} \Rightarrow 2y &= p \\ y &= \frac{p}{2} \end{aligned}$$

check 2<sup>nd</sup> order condition!

$$\frac{d^2\pi}{dy^2} = -2 < 0 \quad \checkmark$$

check shutdown

$$c(y) = y^2$$

$$AVC(y) = \frac{y^2}{y} = y$$

shutdown if

$$AVC(y) > p$$

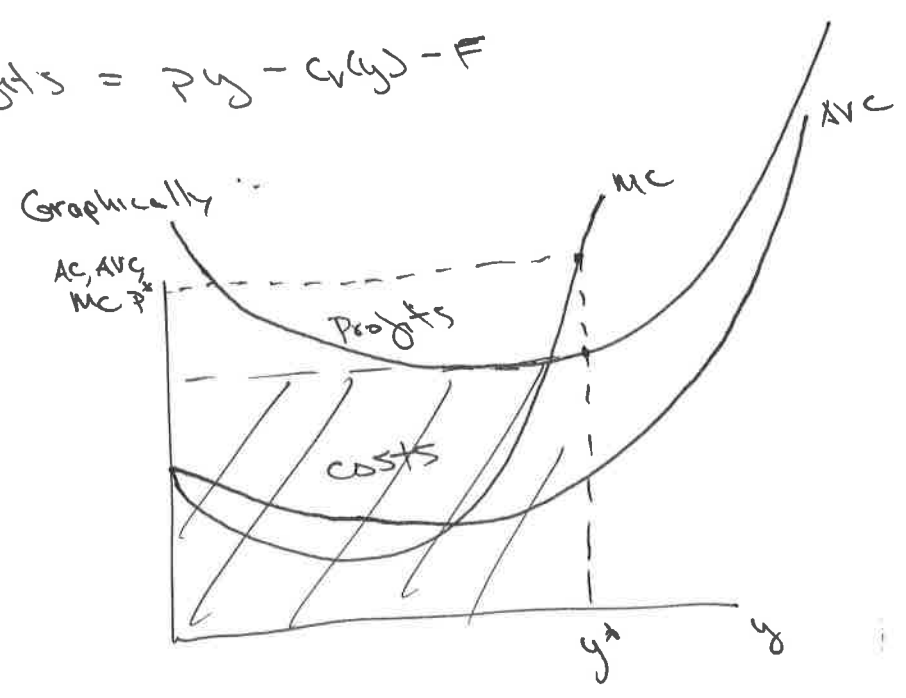
$$y > p$$

$$\frac{p}{2} > p$$

→ not shutdown for any  $p > 0$

# Profits and Producer Surplus

$$\text{Profits} = py - c_v(y) - F$$



$$\text{Revenue} = p \times y$$

$$\text{costs} = c(y) = AC(y) \times y$$

$$\begin{aligned} \text{Profits} &= \text{Rev} - \text{costs} \\ &= py - c(y) \end{aligned}$$

Producer surplus is related to profits

$$\begin{aligned} \rightarrow \text{PS} &= \text{revenue} - \text{variable costs} \\ &= py - c_v(y) \end{aligned}$$

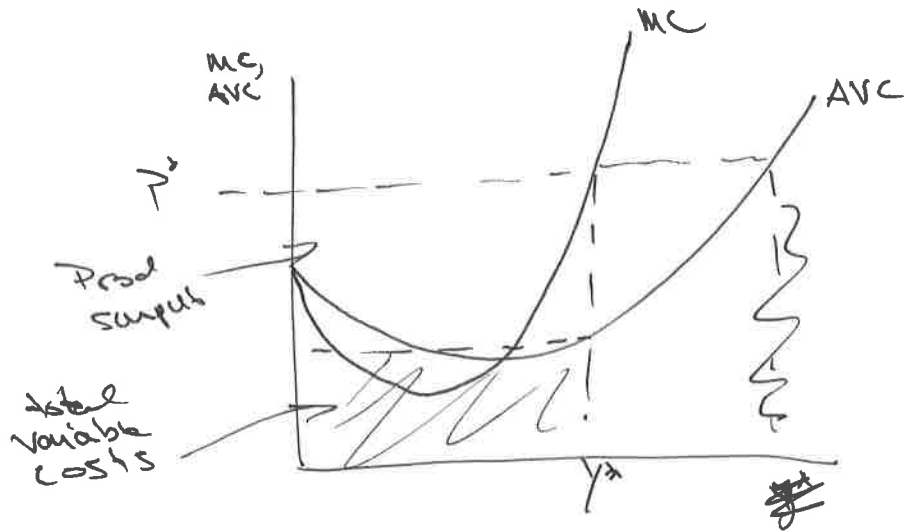
→ exclude fixed costs b/c pay those w/  
 $y=0$  or not → so they are  
 excluded from the surplus from  
 producing

2 ways to see producer surplus graphically:

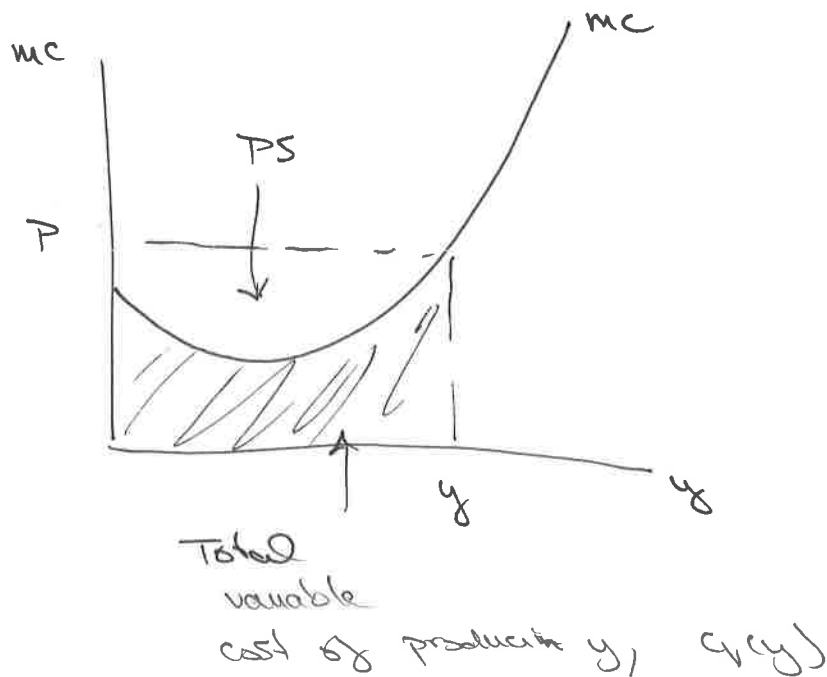
1) Diff btwn revenue and total variable cost

$$\text{revenue} = p \times y$$

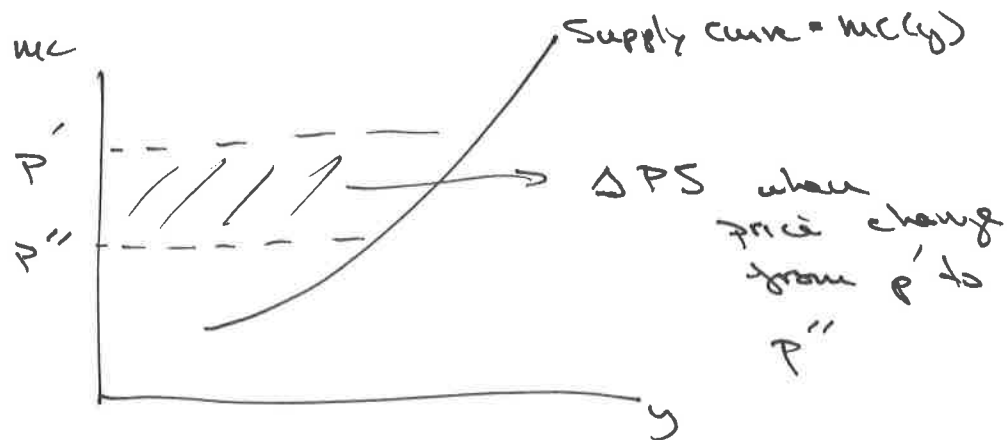
$$\text{total variable cost} = AVC(y) \times y$$



2) Using just the MC curve!



→ This 2<sup>nd</sup> way makes it easier to see  $\Delta$  in PS



### Long run supply

→ In the long run, all factors are variable

$$\pi = py - \underbrace{c(y)}_{\text{long-run costs}}$$

FoC:

$$p = \underbrace{MC(y)}_{\text{LR marginal cost}}$$

this equation yields the LR supply curve

→ Shutdown decision now based on LAC  
 (ok fixed costs not fixed):

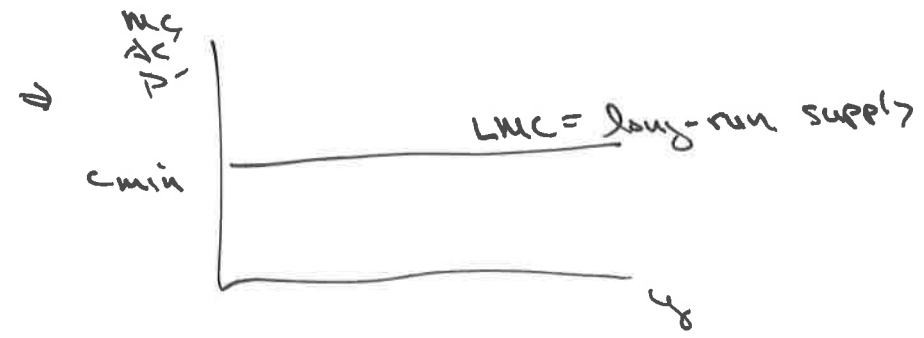
$$\text{shut down if } p < \frac{c(y)}{y}$$

$$p < LAC(y)$$



A special case: constant LR avg. costs

→ w/ constant returns to scale, the LR MC curve = the LR AC curve



→ firm will supply any amt at  $p = c_{min}$ ,  
zero if  $p < c_{min}$ , infinite if  $p > c_{min}$

→ here we see again that the scale of production is indeterminate w/ CRS